

# SMT, CAD & Applications



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## Satisfiability modulo theories solving

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- ▶ Termination proving
- ▶ Controller synthesis
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- ▶ Product design automation
- ▶ And growing ...

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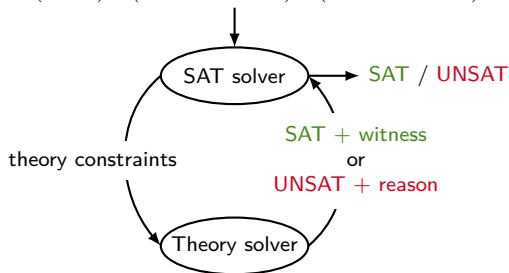
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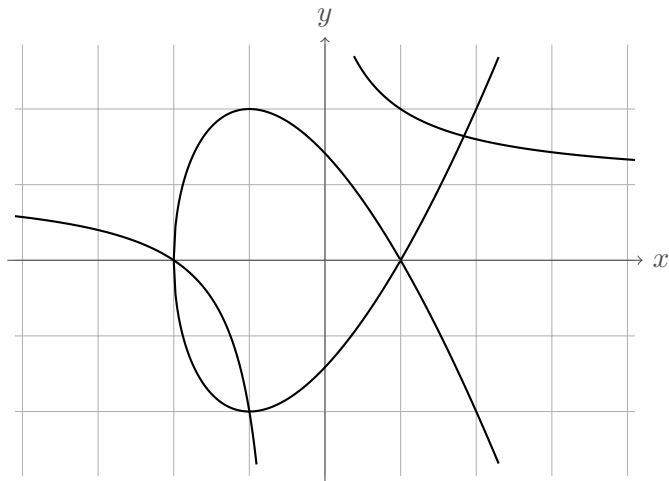
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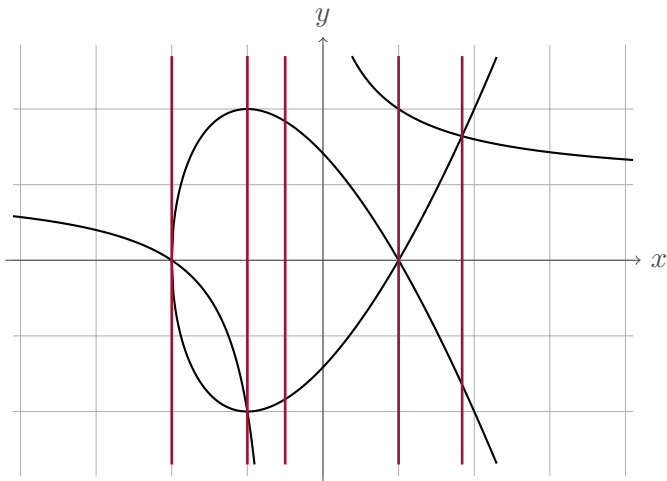
$$\varphi = (x > 0) \wedge (x^2 > 0 \vee x < 0) \wedge (x^3 < 0 \vee x = 3)$$



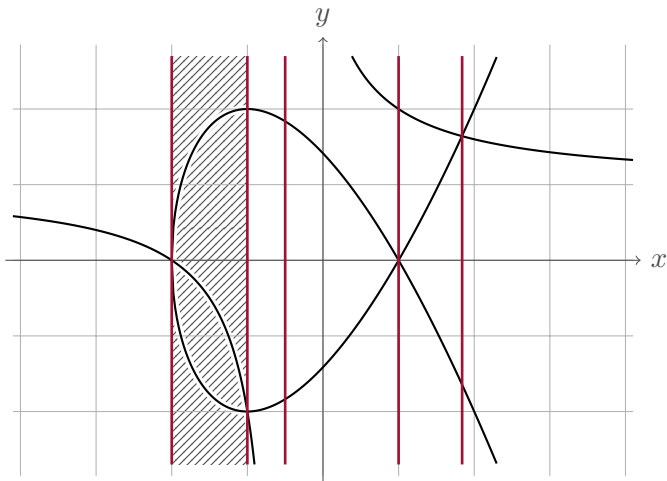
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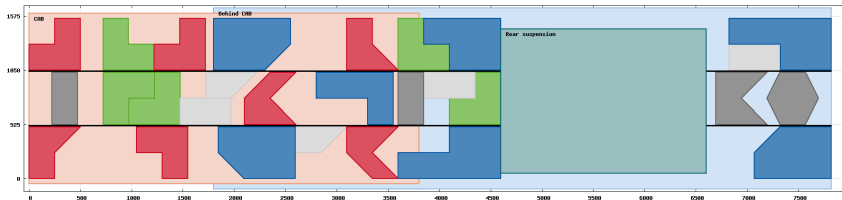


## Cylindrical Algebraic Decomposition



# Applications

- ▶ Configuration management (automotive)
- ▶ Geometric layout planning (automotive)



- ▶ Optimal deployments of cloud application (Zephyrus 2)
- ▶ Strategies for cooperating robots (RoboCup Logistics League)
- ▶ Generalization of counterexamples (MCSAT)
- ▶ Quantifier elimination